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September 15, 1999

Assistant Commissioner for Patents  
Box NEW PATENT APPLICATION  
Washington, D.C. 20231

Jc678 U.S. PTO  
09/396052  
09/15/99

Re: New Patent of  
JOHAN OLOF ANDERS **ROBERTSSON** AND  
ANDREW **CURTIS**  
entitled, "**Seismic Detection Apparatus and Related Method**"  
(Our Reference No. 57.0307)

Sir,

Enclosed for filing in the U.S. Patent and Trademark Office is the above-identified new patent application with 24 pages of text including 5 pages of claims (1-27) and an Abstract, plus 8 sheets of drawings (Figs 1-8), and an unexecuted Declaration.

The filing fee is calculated as follows:

Basic Filing Fee	\$ 760.00
Total Claims = <u>27</u>	
Excess over 20 = <u>7</u> X \$18.00	126.00
Independent Claims = <u>3</u>	
Excess over 3 = <u>0</u> X \$78.00	
<b>Total Fees</b>	<b>\$886.00</b>

It is respectfully requested that a filing date bearing today's date be assigned to this application in accordance with 37 CFR §§1.10, which permits express mail filing and late filing of the oath or declaration and filing fee, respectively.

The Commissioner is hereby authorized to charge Deposit Account **N°. 19-0615** in the amount of **\$886.00** to cover the above-calculated fees and any other filing fees that may be required under 37 C.F.R. §1.16. Should this amount be incorrect, the Commissioner is hereby authorized to charge or credit any deficiency or overpayment to Deposit Account **N°. 19-0615**

Two copies of this transmittal letter are enclosed for PTO accounting use.

Respectfully submitted,

By WBS  
William B. Batzer  
Registration No. 37,088

# PATENT APPLICATION

## SEISMIC DETECTION APPARATUS AND RELATED METHOD

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### Priority Information:

UK Application No. 9820049.6, filed 16 September 1998; and  
UK Application No. 9906995.7, filed 29 March 1999.

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## Seismic Detection Apparatus and Related Method

This invention relates to seismic detection apparatus and to a  
5 method of analyzing data acquired by such apparatus.

### BACKGROUND OF THE INVENTION

10 In seismic detection, a seismic source signal propagates through  
different rock substrates or strata within the earth, so producing  
compression wave (P-waves) and shear wave (S-waves) energy which  
can be analyzed to determine the direction and extent of geological  
features in strata.

15 Generally a seismic source signal is produced, either on land, sea,  
or in a borehole, the source signal usually being produced as  
either acoustic or elastic energy. Some of the energy radiates  
downward through geological layers within the earth and is  
reflected in varying proportions at different layer boundaries and  
20 this reflected energy can be detected at the surface. Some of the  
energy within the seismic source signal propagates directly along  
the ground producing a wave signal known as ground-roll. To detect  
the acoustic reflections which are in the form of P-waves and S-  
waves, a linear or areal array of geophones is often used to  
25 reinforce the reflected energy and to attenuate the energy  
associated with ground-roll so that a good signal to noise ratio  
can be achieved for the reflected wave components of interest.

It is desirable to be able to separate the P-wave and S-wave  
30 components of an elastic wave field as the separated components can  
be used more effectively to identify different characteristics than  
when combined. It is an aim of the present invention to provide  
improved separation of seismic signals into P-wave and S-waves.

Methods have been described which use three or more sensors in close proximity (e.g. less than 1 meter) for determining certain ground characteristics very close to the sensors. For example, in published European Patent Application 0 455 091 A2 (Application No. 91106459.0), a method is described which uses relatively closely spaced "oscillation sensors" to determine the "laminar structure and other characteristics of [the] ground." However, this method only provides information about characteristics of the ground within a distance from the sensor array of the order of the maximum wavelength of the surface waves (hereinafter referred to as the "near-site ground structure"). Moreover, the method relies on sensing "microseisms" which is believed to refer to naturally occurring seismic activity. Thus, the published application does not disclose a method using seismic energy from a man-made seismic source, nor does it teach a method of sensing the components used to process reflected waves. Rather the method is only concerned with ground-roll type waves and does not teach or suggest a method suitable for hydrocarbon exploration using seismic energy reflected from man-made seismic sources.

#### SUMMARY OF THE INVENTION

According to one aspect of the present invention, there is provided seismic detection apparatus comprising seismic detection means capable of detecting a plurality of seismic components over a selected volume.

Preferably the seismic detection means comprises a plurality of receivers spaced apart to enclose the selected volume. The receivers may include hydrophones, geophones, accelerometers or a combination of these, and preferably are adapted to detect seismic

signals along three mutually orthogonal axes. Thus the receivers may be provided by three-component geophones.

Preferably the selected volume is formed by at least three  
5 receivers spaced within a plane and at least one receiver placed external to the plane, thereby to enclose the selected volume over which measurement of seismic signals occurs.

In accordance with the invention, the receivers can be spaced to  
10 form a tetrahedron with three receivers spaced to define a triangle within the plane and a fourth receiver placed external the plane but in line with the centroid of the triangle. Other configurations of spaced apart receivers may be used depending on the characteristics of the wavefield being measured, for example  
15 receivers may be spaced to form an octahedral volume, a cubic volume, or a spherical volume. Certain shaped volumes may be more appropriate for different uses, for example receivers spaced to form an octahedral volume may be more appropriate for use with permanent downhole sensors.

20 The seismic detection apparatus in accordance with the present invention is suitable for use on the ground surface or ocean bottom. When used on the ground surface, the enclosed volume can be achieved by placing one receiver further below the surface of  
25 the other receivers, for example by burying it beneath the surface. With marine and ocean bottom surveys, the volume may be defined by tethering the receivers at different water depths, for example by placing three receivers spaced apart at the same depth, and a fourth receiver at a different depth. The seismic detection  
30 apparatus according to the present invention is also of use in seismic detection in transition zones such as swamps and marshes, where again tethering of the receivers at different depths will define the enclosed volume.

5 The apparatus may also have all the receivers incorporated into one  
body for attaching to a wireline and using downhole, or for using  
permanently downhole. Such a permanent sensor is of particular  
10 advantage where monitoring of a reservoir or other geological  
feature over time is required. This may be appropriate when  
monitoring fluid flow occurring within a reservoir as permanent  
sensors can be used to detect natural seismicity resulting from  
fluid opening and closing micro-fissures within the substrates and  
15 producing micro-earthquakes. Whilst these micro-earthquakes  
produce very weak broadband signals, by use of permanent sensors,  
this activity can be detected and production adapted by remedial  
action such as acid to remove carbonate deposits, or fracturing  
rock with high pressure steam or water, so as to improve production  
efficiency.

20 Preferably the apparatus further comprises processing means which  
analyses detected seismic components from individual receivers to  
separate P-wave components from S-wave components. The processing  
means may be provided at substantially the same location as the  
receivers to allow for on-site processing, or remote from the  
receivers to allow off-site processing.

25 In surveys of the vertical component of seismic data, the receivers  
may be adapted to detect components along one axis and orientation  
of the receivers selected so as to permit processing of one-  
component data to identify P-wave components. Therefore the  
receivers may be provided by one-component geophones.

30 Preferably the spacing of the receivers is selected to be smaller  
than the wavelength of the detected seismic components. A  
preferred spacing is less than 1 m, more preferably between 0.05m  
and 0.50m, although larger spacings of up to a third of the

shortest detected wavelength are possible, and thus the range may be between 1.5 and 15m.

In use, the apparatus may be operated to detect seismic signals over a time period of the order of five seconds where P-wave components are of principal interest, with any marginal S-wave component detected at that time being used to produce improvements in the signal to noise ratio.

Where a detection time of the order 10 to 15 seconds is used, both P-wave and S-wave components will be detected within the seismic signals and may be separated for multi-component inversion yielding images of reservoirs and other geological formations, and full reservoir characterization.

In accordance with another aspect of the invention, there is provided a method of processing seismic data comprising acquiring seismic data relating to a wavefield over a selected volume of acquisition, and measuring the curl and divergence of the wavefield from the seismic data, to thereby identify seismic components within the seismic data.

As P-waves are curl free and S-waves divergence free, this allows the separate identification of P-wave and S-wave components. Up-going and down-going wavefield components in boreholes may also be identified from the seismic data. Attenuation of unwanted seismic components from data acquired downhole is also enabled, and noise sources such as ground roll, airwave and inter-sensor perturbations can be removed from the data by signal processing.

The method preferably further comprises averaging the curl and divergence over the selected volume of acquisition, and where appropriate acquiring seismic data over a selected period of time.

Additionally the method may further comprise defining the selected volume of acquisition to be small compared to the wavelength of seismic waves to be detected.

5

As described above, in a seismic acquisition at a free surface, the constraints imposed by the free surface enable the reduction of the acquisition volume to a acquisition surface where all receivers are located in a plane.

10

In another aspect of the invention, the representation theorem based filters used for removing multiples from Ocean Bottom Cable data as described in the Published UK Patent Application GB 2 333 364 A (Published 21 July 1999) is modified to provide a method of separating the seismic data acquired with the planar receiver configuration above into up- and downgoing wavefield.

15

In a variant that is particularly suitable for hydrocarbon exploration seismic acquisitions at a free surface or fluid/solid boundary, the volume formed by the receivers can be reduced to a plane. Hence, three 3-component receivers can be used in combination with the free surface (or fluid/solid) condition constraints to advantageously determine approximations to the spatial and temporal derivatives local to the receivers

20

(hereinafter the "full wavefield"). The receivers should be adapted to measure the seismic energy from a seismic source that has been reflected from one or more subterranean earth structures outside the near-site ground structure.

25

According to a further aspect of the invention, each of the receivers are one-component geophones and a fourth seismic receiver is located less than about 1 meter from the other three seismic receivers.

30



A method for hydrocarbon exploration is also provided that includes imparting seismic energy into the earth that travels through the earth and reflects off of one or more subterranean earth structures outside the near-site ground structure. At least three seismic receivers are positioned substantially in a plane at or near the earth surface, and the seismic receivers are spaced less than about 1 meter from each other to form a receiver cluster. The received seismic energy is stored and analyzed to determine characteristics of one or more hydrocarbon reservoirs.

Preferably, the curl and divergence of the wavefield is determined from the seismic data, thereby identifying seismic components within the seismic data.

Preferably, the P-wave and S-wave components are separately identified, the up-going and down-going wavefield components are identified from the seismic data, and unwanted seismic components from seismic data is attenuated.

Preferably, the curl and divergence is averaged over the selected plane or volume of acquisition, and the selected plane or volume of acquisition is defined to be small compared to the wavelength of seismic waves to be detected.

These and other features of the invention, preferred embodiments and variants thereof, possible applications and advantages will become appreciated and understood by those skilled in the art from the detailed description and drawings following hereinafter.

## BRIEF DESCRIPTION OF THE DRAWINGS

FIG. 1 shows an example of the distribution of seismic data over a specified period of time;

5

FIG. 2 shows an example of a seismic data acquisition and system according to the present invention;

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FIG. 3 shows one embodiment of seismic detection apparatus according to the present invention;

FIG. 4 shows a second embodiment of seismic detection apparatus according to the present invention;

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FIG. 5 shows a tetrahedron used in explanation of a processing method according to the present invention;

20

FIG. 6 shows a planar configuration of receivers according to the present invention;

20

FIG. 7 shows a top view of a configuration of four 1C geophones in a plane that can be used to measure the divergence on the Earth's free surface according to the present invention; and

25

FIG. 8 summarizes a processing method based on a planar receiver arrangement according to the present invention.

## MODE(S) FOR CARRYING OUT THE INVENTION

30

In Figure 1, a typical hodogram of a three component marine shot gather survey is shown, where the x axis is the offset in meters and the y axis is time in seconds from the generation of a source signal at  $t=0$ . A hodogram displays the different seismic

components detected over a specified time-window. The first arrivals around  $t=1s$  predominantly comprise P-waves 10, 10'. Near-surface scattering and channeling in slower near-surface layers are revealed in the P-wave arrivals contained in the hodogram through some degree of elliptical motion. Following the P-wave arrivals is a relatively quiet section 12, 12' (where deeper reflections can be observed) until the S-wave arrivals 14, 14' are observed near  $t=3s$ . The S-waves also scatter and become channeled in the near-surface which causes ellipticity in the hodogram.

Following the S-wave arrivals are elliptically polarized Rayleigh waves 16, 16' (ground-roll). The innermost "cone" 20 of the section consists of strongly scattered energy that typically masks deeper reflections.

Noise in seismic data to a large degree comprises source-generated ground-roll and S-waves. Separating P-wave data from S-wave data is useful to reduce noise attenuation. Also P-wave data may be of primary interest with the complete removal of S-waves being preferred, for example in shallow seismic imaging for engineering or environmental purposes.

Measuring the P-wave and S-wave components of an elastic wavefield separately has several advantages. First, separation of P-waves and S-waves enables better and more accurate analysis of each separated component thus improving moveout analysis and Amplitude Versus Offset (AVO) analysis. Secondly heterogeneity in the near-surface (as well as deeper down in the crust) and rough surface topography, scatter S-waves to a greater extent than P-waves, with scattered S-waves significantly contributing to noise in seismic reflection data.

Figure 2 is a schematic illustration of a seismic data acquisition and processing system. Seismic sources 110, 112, and 114 are depicted which impart seismic energy into the earth at its surface 126 at predetermined times upon command of a controller (not shown). The seismic sources may comprise impulsive sources (such as explosives, or in the marine environment, airguns) or vibratory sources. While three sources are depicted for simplicity, other numbers of sources, including a single source, could be used. The seismic data acquisition could be carried out on land, marine, or transition-zone environments. In the case of marine acquisition, 126 would depict the ocean bottom, and the sources 110, 112 and 114 would typically be submerged at a predetermined depth near the water surface (not shown). In this case receivers 116, 118 and 120 can be in an ocean bottom cable. In the case of land acquisition, surface 126 is the ground, and truck mounted vibrators can be used as sources 110, 112 and 114. The seismic energy imparted by the sources travels through the earth in the form of both p and s waves; this is schematically depicted in Figure 2 as, for example, arrow 134. The energy reflects off of certain subterranean surfaces, here depicted as surface 122 and surface 124, and eventually reach and are detected by receivers 116, 118, and 120 as depicted, for example, by arrow 138. According to the preferred embodiment, receivers 116, 118 and 120 will be geophones, but other suitable receivers such as optical sensors could be used. Note that receivers 116, 118 and 120 in Figure 2 correspond to the receivers and geophones depicted in Figures 3, 4, 6, and 7. Although only three receivers are shown in Figure 2, there could be more receivers used in a particular embodiment. For example, in the embodiments shown in Figures 3, 4 and 7, at least four receivers are used.

Referring again to Figure 2, the apparatus shown is being used for seismic exploration of hydrocarbon reservoirs. Cap rock 128 is

relatively impermeable to the hydrocarbon substance. The hydrocarbon substance is thereby trapped in hydrocarbon reservoir 130. Hydrocarbon reservoir 130 is typically made up of a reservoir rock (for example sandstone in a sand channel) and the interface  
5 between it and the cap rock 128 reflects the seismic energy back to the receivers as depicted by arrow 138. Also shown in Figure 2 is ground roll (e.g. Rayleigh waves) which is schematically depicted as arrow 136. Ground roll travels in the near-surface region and does not penetrate to depths necessary for locating and  
10 characterizing hydrocarbon reservoirs such as reservoir 130.

Receivers 116, 118, and 120 convert the seismic energy into electrical signals and transmit these signals to a central recording unit 140. In the case of land acquisition this central  
15 recording unit 140 is typically located at the local field site, and in marine acquisition it is typically located on the vessel used to tow the sources and receivers (not shown). Once the central processing unit 140 performs correlation and other desired processing, it typically stores the data in the form of time-domain  
20 traces on a magnetic tape. The data, in the form of magnetic tape is later sent for processing and analysis to a seismic data processing center, typically located in some other geographical location. The data transfer from the central recording unit 170 in Figure 2 is depicted as arrow 176 to a data processor 180.

Figure 3 shows one embodiment of a seismic detection apparatus according to the present invention, with four three-component detectors, such as geophones or hydrophones, being placed to form an enclosed tetrahedral volume. Geophones are velocity motion  
30 sensors, with hydrophones being pressure sensors. Geophones 22, 24, 26 are arranged in a horizontal plane 30 with each geophone being spaced the same distance from the other two geophones, so as to form an equilateral triangle. The fourth geophone 32 is placed

vertically below the centroid 34 of the equilateral triangle formed by geophones 22, 24, 26. Placing of geophone 32 external to the horizontal plane 30 is achieved by positioning the horizontal plane 30 on or close to the Earth's surface with the fourth geophone 32 dug to a position well below surface. Within a marine, ocean bottom or swamp environment, the arrangement of receivers is achieved by tethering three hydrophones and/or geophones at one depth and one hydrophone and/or geophone at a different depth.

10 An ideal tetrahedral volume is not essential, and thus for example two geophones placed external to horizontal plane 30 can be used.

The geophones 22, 24, 26 are positioned one meter apart, although spacing will vary depending on the surrounding rock substrate and how fast waves travel within the substrate. The spacing of the geophones to form an enclosed volume 36 is chosen so that the wavefield is detected on a scale which is smaller than the wavelengths of interest. For wave frequencies of between 50 to 100 Hz with velocity ranging from 300-2000 m/s, the wavelength tends to be in the range 5 to 50 m. To record the wavefield over such a range, the spacing of the geophones is generally a third of the wavelength and generally in the range 1.0m to 15m, although may be as small as 0.05 m. The tetrahedron arrangement shown in Figure 3 uses the minimum number of geophones required to define an enclosed volume, although other configurations with more geophones are possible, such as those forming an octahedron, cube or sphere.

The use of four three-component geophones distributed as shown in Figure 3 allows the separation of the wavefield into P-waves and S-waves. After the seismic data has been recorded either where acquisition of data is occurring or remote from the geophones, differences in geophone coupling can be removed by normalizing separately the responses of each component at the corners of the

tetrahedron. If required, more accurate compensation for coupling differences can be obtained by using information from adjacent tetrahedral arrays of geophones, while preserving the offset varying character of the seismic data. The geophone coupling may also be frequency dependent varying from geophone to geophone.

The three-component geophones 22, 24, 26, 32 detect components of the seismic signal at three orthogonal axes. By measuring the curl of a displacement field  $\mathbf{u}(x, t)$  within the enclosed volume 36 and the divergence of the displacement field within the volume 36, it is possible to separate out the P-wave and S-wave components as P-waves have zero curl and S-waves have zero divergence.

With the array of geophones shown in Figure 4, the four geophones 40, 42, 44, 46 are one-component geophones. The array encloses a tetrahedral volume 50 once more, but the axis along which each one-component geophone measures is calculated and precisely implemented when positioning the apparatus to ensure that the divergence can be deduced from the single components measured. Measuring with single component geophones provides less information about the seismic signals. However at present 90% of seismic surveys only monitor the vertical component, and the apparatus of Figure 4 when used with a listening time of five seconds allows a substantial improvement in the signal to noise ratio if looking principally for P-wave components.

Once data are acquired using the geophone array enclosing a volume, separation of the wave-field into P-waves and S-waves or improvement of the signal to noise ratio for P-wave components, can be undertaken by use of the method described below.

The elastic wave equation for a displacement field  $\mathbf{u}(x, t)$  in an isotropic medium with Lamé parameters  $\lambda$  and  $\mu$  and density  $\rho$  can be written as:

$$5 \quad [1] \quad \rho \ddot{\mathbf{u}} = \mathbf{f} + (\lambda + 2\mu) \nabla(\nabla \cdot \mathbf{u}) + \mu \nabla \times (\nabla \times \mathbf{u})$$

Here  $\mathbf{f}$  denotes a distribution of body forces. Lamé's theorem (Aki and Richards, 1980) states that there exist potentials  $\Phi$  and  $\Psi$  of  $\mathbf{u}$  with the following properties:

$$10 \quad [2] \quad \mathbf{u} = \nabla \Phi + \nabla \times \Psi ,$$

$$[3] \quad \nabla \cdot \Psi = 0 ,$$

$$15 \quad [4] \quad \ddot{\Phi} = \frac{\Phi}{\rho} + \alpha^2 \nabla^2 \Phi ,$$

$$[5] \quad \ddot{\Psi} = \frac{\Psi}{\rho} + \beta^2 \nabla^2 \Psi ,$$

where  $\alpha$  and  $\beta$  are the P- and S- velocities. An elastic wavefield  $\mathbf{u}$  can thus be decomposed into its P- and S-wave components,  $\nabla \Phi$  and  $\nabla \times \Psi$ , respectively. Equations [2] and [3] yield

$$[6] \quad \nabla \cdot \mathbf{u} = \nabla^2 \Phi ,$$

$$25 \quad [7] \quad \nabla \times \mathbf{u} = \nabla \times \nabla \times \Psi$$

(Råde, L., and Westergren, N., 1988, BETA  $\beta$  Mathematics Handbook: Student litteratur, Lund.). By measuring the curl and the



divergence of an elastic wavefield we can thus measure the P- and S-wave components separately.

The technique for P- and S-wave separation is based on recording the elastic wavefield around a small volume as compared to the wavelength. The volume may be of arbitrary shape, but the equations for wavefield separation are simplified if the volume has a known deterministic shape such as that of a tetrahedron, cube, octahedron or a sphere. A co-ordinate system that is appropriate for the geometry employed simplifies the equations further. The discussion of the method below uses a tetrahedron and the formulae are derived in Cartesian co-ordinates.

Figure 5 shows a tetrahedron with corner points  $\mathbf{P}_1$ ,  $\mathbf{P}_2$ ,  $\mathbf{P}_3$ , and  $\mathbf{P}_4$ . We denote the Cartesian co-ordinates of point  $\mathbf{P}_i$  by  $(x_i, y_i, z_i)$ .

Let  $\overline{\mathbf{P}_j\mathbf{P}_i}$  denote the vector that starts at  $\mathbf{P}_i$  and ends at  $\mathbf{P}_j$ . The volume of the tetrahedron in Figure 5,  $V_{\text{tetra}}$ , can be calculated from the absolute value of the determinant of the matrix  $M$  with the vectors  $\overline{\mathbf{P}_2\mathbf{P}_1}$ ,  $\overline{\mathbf{P}_3\mathbf{P}_1}$ , and  $\overline{\mathbf{P}_4\mathbf{P}_1}$  as rows:

$$[8] \quad V_{\text{tetra}} = \frac{1}{6} |\det M|.$$

Gauss' theorem states

$$[9] \quad \iiint_V (\nabla \cdot \mathbf{u}) dV = \iint_S \mathbf{u} \cdot d\mathbf{S}$$

or alternatively,

$$[10] \quad \iiint_V (\nabla \times \mathbf{u}) dV = \iint_S \mathbf{u} \times d\mathbf{S}.$$

If the dimensions of the tetrahedron configuration in Figure 5 are small compared to the wavelength of  $\mathbf{u}$ , the mean values of the curl and divergence in equations [9] and [10] can be calculated from:

$$[11] \quad \nabla \cdot \mathbf{u} \approx \frac{1}{V_{\text{tetra}}} \iiint_V (\nabla \cdot \mathbf{u}) dV$$

and

$$[12] \quad \nabla \times \mathbf{u} \approx \frac{1}{V_{\text{tetra}}} \iiint_V (\nabla \times \mathbf{u}) dV .$$

Moreover, the surface integrals on the right hand side of equations [9] and [10] reduce to four surface integrals respectively, over plane triangular surfaces.

Since the normal to the surface of the tetrahedron does not vary over each of the triangular sub-surfaces, equation [9] becomes

$$[13] \quad \begin{aligned} \iiint_V (\nabla \cdot \mathbf{u}) dV = & \iint_{S_{123}} \mathbf{u} dS \cdot \mathbf{n}_{123} \\ & + \iint_{S_{243}} \mathbf{u} dS \cdot \mathbf{n}_{243} \\ & + \iint_{S_{142}} \mathbf{u} dS \cdot \mathbf{n}_{142} \\ & + \iint_{S_{134}} \mathbf{u} dS \cdot \mathbf{n}_{134} , \end{aligned}$$

where  $\mathbf{n}_{ijk}$  is the outward unit normal to the triangular subsurface  $S_{ijk}$  with corner points  $\mathbf{P}_i$ ,  $\mathbf{P}_j$  and  $\mathbf{P}_k$  (see Figure 5).

Where the side of the tetrahedron is small compared to the wavelength of the elastic wavefield, the value of  $\mathbf{u}$  at any point on one of the triangular surfaces of the tetrahedron can be calculated by linear interpolation of the wavefield between the three corner points of the triangle. The surface integral over  $S_{ijk}$  (using linear interpolation between  $\mathbf{P}_i$ ,  $\mathbf{P}_j$  and  $\mathbf{P}_k$ ) then reduces to

$$[14] \quad \iint_{S_{ijk}} \mathbf{u} dS = \frac{A}{3} (x_i + x_j + x_k, y_i + y_j + y_k, z_i + z_j + z_k),$$

where  $A$  is the area of  $S_{ijk}$ . Since  $A \mathbf{n}_{ijk} = \overline{\mathbf{P}_j \mathbf{P}_i} \times \overline{\mathbf{P}_k \mathbf{P}_i} / 2$  we have

$$[15] \quad \iiint_V (\nabla \cdot \mathbf{u}) dV = \frac{1}{6} [$$

$$(x_1 + x_2 + x_3, y_1 + y_2 + y_3, z_1 + z_2 + z_3) (\overline{\mathbf{P}_2 \mathbf{P}_1} \times \overline{\mathbf{P}_3 \mathbf{P}_1})$$

$$+ (x_2 + x_4 + x_3, y_2 + y_4 + y_3, z_2 + z_4 + z_3) (\overline{\mathbf{P}_4 \mathbf{P}_2} \times \overline{\mathbf{P}_3 \mathbf{P}_2})$$

$$+ (x_1 + x_4 + x_2, y_1 + y_4 + y_2, z_1 + z_4 + z_2) (\overline{\mathbf{P}_4 \mathbf{P}_1} \times \overline{\mathbf{P}_2 \mathbf{P}_1})$$

$$+ (x_1 + x_3 + x_4, y_1 + y_3 + y_4, z_1 + z_3 + z_4) (\overline{\mathbf{P}_3 \mathbf{P}_1} \times \overline{\mathbf{P}_4 \mathbf{P}_1})]$$

Equivalently, the curl of  $\mathbf{u}$  in  $V$  can be calculated as

$$[16] \quad \iiint_V (\nabla \times \mathbf{u}) dV = \frac{1}{6} [$$

$$(x_1 + x_2 + x_3, y_1 + y_2 + y_3, z_1 + z_2 + z_3) \times (\overline{\mathbf{P}_2 \mathbf{P}_1} \times \overline{\mathbf{P}_3 \mathbf{P}_1})$$

$$\begin{aligned}
& + (x_2 + x_4 + x_3, y_2 + y_4 + y_3, z_2 + z_4 + z_3) \times (\overline{\mathbf{P}_4 \mathbf{P}_2} \times \overline{\mathbf{P}_3 \mathbf{P}_2}) \\
& + (x_1 + x_4 + x_2, y_1 + y_4 + y_2, z_1 + z_4 + z_2) \times (\overline{\mathbf{P}_4 \mathbf{P}_1} \times \overline{\mathbf{P}_2 \mathbf{P}_1}) \\
& + (x_1 + x_3 + x_4, y_1 + y_3 + y_4, z_1 + z_3 + z_4) \times (\overline{\mathbf{P}_3 \mathbf{P}_1} \times \overline{\mathbf{P}_4 \mathbf{P}_1}) ]
\end{aligned}$$

Finally, the average values of the divergence and curl of  $\mathbf{u}$  within  $V$  are obtained from equations [11] and [12].

In this way, the divergence and curl of a wavefield can be calculated from a set of closely spaced measurements distributed in all spatial directions. A minimum of four measurement points is needed. The volume that is bounded by planes connecting these points is generally a tetrahedron and where the dimensions of the tetrahedron are small with respect to the wavelength of the wavefield, an assumption that the wavefield varies linearly along each side of the enclosed volume is possible. The average divergence and average curl can then be efficiently calculated using Gauss' theorem.

For instance the average divergence inside the tetrahedron is calculated from the volume integral of the divergence of the wavefield over the tetrahedron, divided by its volume. The volume integral can in turn be converted to four surface integrals over each side of the tetrahedron by using Gauss' theorem. If the wavefield varies linearly over each side, these surface integrals are simply the volume of a prism where the base of the prism is the surface area and the heights of the three corners are the magnitude of the wavefield in the respective corners projected onto the normal of the surface.

The average curl of the wavefield is evaluated similarly. The same procedure can be used to calculate average curl and divergence over more general volumes.

5   Uncertainties in the actual geometry can be eliminated by allowing the exact locations of  $\mathbf{P}_1$ ,  $\mathbf{P}_2$ ,  $\mathbf{P}_3$ , and  $\mathbf{P}_4$  to vary subject to either minimizing equation [16] over a window(s) with an identified P-event and/or minimizing equation [15] over S-events. This technique may also serve as an alternative means for adjusting for  
10   the differences in geophone coupling over the tetrahedron.

For anisotropic media the decomposition of  $\mathbf{u}$  into P- and S-wave components as described by equations [2], [3], [4] and [5] is strictly not valid since the (quasi) P- and S-waves in anisotropic  
15   media both have compressional and shear components. However, this is of secondary importance and the theory above will be approximately valid for most practical cases.

In heterogeneous media, the heterogeneities act as secondary  
20   sources and scatter the wavefield. The separation of a wavefield into P-waves and S-waves is not strictly valid in the vicinity of a source. However the P/S separation technique described herein is generally applicable for common heterogeneous and anisotropic Earth materials, as well as for isotropic materials as discussed above.

25   With the apparatus and associated method, P-wave and S-wave components in seismic data can be separated.

In addition attenuation of near-surface scattering is possible as  
30   much noise is of S-wave character and where the primary interest is to record P-wave data, S-waves can be removed by employing the configuration of four one-component geophones as shown in Figure 4.

The present invention is particularly well-suited for seismic techniques applied to hydrocarbon exploration. However, the present invention also finds application in environmental, engineering and groundwater exploration and imaging. For such applications, it is typically of interest to image or detect very shallow structures, as shallow as 1-100m. Near-surface generated noise is particularly severe in these applications and a configuration of receivers such as in Figure 4 is particularly advantageous for shallow seismics.

The invention also allows for the attenuation of ground-roll. Since ground-roll can be elliptically polarized, it will appear both in the separated P- and S-wave sections, but with lower amplitude in the separated P-wave sections.

P- and S-wave separation is of particular use for marine seismic data recorded at the seafloor, since the near-surface at the seafloor is generally is of a more homogeneous character than at land. The technique is of use in removing Scholte waves that typically contaminate ocean data. Moreover, measurements of the wavefield over a volume also allows for the separation of the wavefield into up- and down-going waves.

Figure 6 shows a receiver arrangement particularly useful for land acquisition. It comprises three 3C (component) geophones 52, 54, 56 arranged in a plane on the surface of the survey terrain. Each component of each geophone is measured independently. Thus, the three geophones are connected to the recording or processing unit 58 via a total of nine channels 60. Cable 62 provides a signal transmission between the groups of geophones.

The preferred spacing of the geophones in this embodiment is chosen in the same manner as described above, i.e. so that the wavefield

is detected on a scale which is smaller than the wavelengths of interest. For wave frequencies of between 50 to 100 Hz with velocity ranging from 300-2000 m/s, the wavelength tends to be in the range 5 to 50 m. To record the wavefield over such a range, the spacing of the geophones is generally a third of the wavelength and generally in the range 1.0m to 15m, although may be as small as 0.05 m.

In this embodiment, the calculations according to the above equations are modified by introducing the free surface boundary condition. This condition constrains the possible solutions for the wavefield such that it is not necessary to employ a (fourth) out-of-plane receiver to sample additional components of the wavefield.

Furthermore the free surface condition is introduced into a formalism known as the elastodynamic representation theorem. This theorem is used for example in the Published UK Patent Application GB 2 333 364 A (Published 21 July 1999) to derive filters for separating up- and downgoing wavefield in the case of ocean bottom acquisition.

Using the representation theorem and the boundary conditions of a solid-air interface, the following equations for up/down going separation of particle velocities  $v$  recorded by the planar receiver arrangement can be obtained:

$$[17] \quad v_v^U(x) = \frac{1}{2} ( v_v(x) - F_{v_3}^{v_v}(x) * v_3(x) ),$$

$$[18] \quad v_3^U(x) = \frac{1}{2} ( v_3(x) - F_{v_v}^{v_3}(x) * v_v(x) ).$$

The subscripts n and m denote indices for the horizontal coordinate axes x and y (for the 2-D case they reduce to x). The filters in equations [17] and [18] are

$$[19] \quad F_{v_3}^{v_v} = -2\partial_v(1 + 2k_\beta^{-2}\partial_\mu^2)g(k_\alpha) + 2k_\beta^{-2}\partial_3^2g(k_\beta) \text{ and}$$

$$[20] \quad F_{v_v}^{v_3} = 2k_\beta^{-2}\partial_v(-2\partial_3^2g(k_\alpha) + (k_\beta^2 + 2\partial_3^2)g(k_\beta)).$$

In particular for the two dimensional (2D) case ( in the frequency-wavenumber domain), using expressions for Green's functions in a homogeneous medium , equations [19] and [20] become:

$$[21] \quad F_{v_z}^{v_x} = \frac{k_x}{2} \left( \left( 1 - 2 \frac{k_x^2}{k_\beta^2} \right) \frac{1}{k_z^{(\alpha)}} - \frac{2}{k_\beta^2} k_z^{(\alpha)} \right) \text{ and}$$

$$[22] \quad F_{v_x}^{v_z} = - \frac{k_x}{2k_\beta^2} \left( 2k_z^{(\alpha)} - 2k_z^{(\beta)} + \frac{k_\beta^2}{k_z^{(\beta)}} \right),$$

where  $k_z^{(\alpha)} = \sqrt{k_\alpha^2 - k_x^2}$  is the vertical wavenumber for P-waves and  $k_z^{(\beta)} = \sqrt{k_\beta^2 - k_x^2}$  is the vertical wavenumber for S-waves.

Filters for combinations of partial derivatives of velocities (e.g. divergence and curl) can be obtained using equations [17] and [18]. Note that for an isotropic elastic medium vertical derivatives of particle velocities recorded at the free surface can be converted to horizontal derivatives (i.e. the 'free surface condition', see J. O. A. Robertsson, "A numerical free-surface condition for elastic/viscoelastic finite-difference modeling in the presence of topography", Geophysics, 1996, Vol. 61, pp. 1921-1934, incorporated herein by reference). A similar transformation of vertical to



horizontal derivatives can be performed at the ocean sea bottom using the fluid/solid boundary condition. A related approach has been disclosed in the Published UK Patent Application GB 2 333 364 A (Published 21 July 1999), incorporated herein by reference.

5

According to another embodiment, shown in Figure 7, one-component sensors can also be used in a closely spaced surface-plane arrangement. Figure 7 is a top view of a configuration of four 1C geophones, 80, 82, 84 and 86 in a plane that can be used to measure the divergence at the Earth's free surface. As mentioned above vertical derivatives can be converted to horizontal derivatives using the free surface condition (or in a marine environment, fluid/solid boundary condition). Therefore, by combining single components of horizontal particle velocity measured by different geophones the divergence can be calculated. Similar configurations of 1C geophones can be designed to measure curl components and/or to include up/down separation of divergence and curl.

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Additionally, the present invention can be implemented as a cluster of sources, rather than as clusters of receivers, according to theorem of reciprocity. In this embodiment the spacing and relative placement of the receivers in Figures 3-6 would instead apply to the spacing and placement of the sources. The analytical method described above could then be used to achieve the objects of the invention.

30

While preferred embodiments of the invention have been described, the descriptions are merely illustrative and are not intended to limit the present invention. For example, although the embodiments have been described in the context of using geophones as the receivers of seismic energy, other types of receivers are contemplated and could be used in the present invention. For

example in Figure 6, receivers 52, 54 and 56 could of the type based on optical and/or laser beams.

## CLAIMS

5        1.    A Seismic detection apparatus comprising:

         a first, second and third receiver, each of the receivers  
         spaced within a plane; and

         a fourth receiver located external to the plane thereby  
         enclosing a selected volume bounded by the first, second,  
10        third and fourth receivers over which measurement of seismic  
         signals occurs.

         2.    A seismic detection apparatus according to claim 1  
         wherein the receivers comprise geophones.

         3.    A seismic detection apparatus according to claim 1  
         wherein the receivers comprise hydrophones.

         4.    A seismic detection apparatus according to claim 2,  
20        wherein the receivers comprise accelerometers.

         5.    A seismic detection apparatus according to claim 2,  
         wherein the seismic detector is adapted to detect seismic signals  
         along three mutually orthogonal axes.

         6.    A seismic detection apparatus according to claim 1,  
         wherein the receivers are spaced to form a tetrahedron, with three  
         receivers spaced to define a triangle within the plane and a fourth  
         receiver placed external the plane but in line with the centroid of  
30        the triangle.

         7.    A seismic detection apparatus according to claim 2,  
         further comprising a processor adapted and configured to analyze

detected seismic components from individual receivers to separate P-wave components from S-wave components.

8. A seismic detection apparatus according to claim 7,  
5 wherein the processor is provided at substantially the same location as the receivers so as to allow for on-site processing.

9. A seismic detection apparatus according to claim 7,  
10 wherein the processor is provided in a location remote from the receiver so as to allow off-site processing of detected seismic components.

10. A seismic detection apparatus according to claim 1,  
15 wherein the receivers are adapted to detect components along one axis and orientation of the receivers is selected so as to permit processing of one-component data to identify P-wave components within the plurality of seismic components.

11. A seismic detection apparatus according to claim 1,  
20 wherein the spacing of the receivers is selected to be smaller than the wavelength of the detected seismic components.

12. A seismic detection apparatus according to claim 1, when  
25 attached to a wireline for placing temporarily downhole.

13. An apparatus for hydrocarbon exploration comprising:

a seismic source adapted to impart seismic energy into the earth at a predetermined time;

at least three seismic receivers each adapted to  
30 measuring the seismic energy from the seismic source that has been reflected from one or more subterranean earth structures outside the near-site structure, the seismic receivers located substantially in a plane at or near the earth surface, wherein

said at least three seismic receivers are spaced less than about 1 meter from each other to form a receiver cluster.

14. An apparatus according to claim 13 further comprising a fourth seismic receiver located less than about 1 meter from the at least three seismic receivers and wherein each of the receivers are one-component geophones.

15. An apparatus according to claim 14 wherein the each of the one-component geophones are positioned in a diamond-shaped pattern and each of the sensed components are in different directions within the plane.

16. An apparatus according to claim 13 wherein each of the receivers are geophones capable of measuring at least three components.

17. An apparatus according to claim 16 wherein the earth surface is the surface of land.

18. An apparatus according to claim 16 wherein the earth surface is the sea bottom.

19. An apparatus according to claim 13 wherein a hydrocarbon reservoir is located near the one or more subterranean earth structures outside the near-site structure.

20. An apparatus according to claim 16, wherein the at least three components of each of the geophones are transmitted to a processing unit to calculate an approximation of the full wavefield at the position of the cluster making use of a free surface boundary condition.

21. A method for hydrocarbon exploration comprising:  
imparting seismic energy into the earth at a predetermined  
time such that the seismic energy travels through the earth and  
reflects off of one or more subterranean earth structures outside  
5 the near-site structure;

positioning at least three seismic receivers  
substantially in a plane at or near the earth surface, wherein  
the seismic receivers are spaced less than about 1 meter from  
each other to form a receiver cluster;

10 receiving seismic energy imparted by the seismic source  
that has been reflected off of the one or more subterranean  
earth structures;

storing seismic data that represents the received seismic  
energy; and

15 analyzing the data such that characteristics of one or  
more hydrocarbon reservoirs can be determined.

22. A method according to claim 21 wherein the step of  
analyzing comprises the step of measuring the curl and divergence  
20 of the wavefield from the seismic data, thereby identifying seismic  
components within the seismic data.

23. A method according to claim 22, wherein P-wave and S-wave  
components are separately identified.

25 24. A method according to claim 23, wherein up-going and  
down-going wavefield components are identified from the seismic  
data.

30 25. A method according to claim 24, wherein the step of  
analyzing further comprises attenuating unwanted seismic components  
from seismic data.

26. A method according to claim 25, wherein the step of analyzing further comprises the step of averaging the curl and divergence over the selected plane or volume of acquisition.

5            27. A method according to claim 26, wherein the step of analyzing further comprises the step of defining the selected plane or volume of acquisition to be small compared to the wavelength of seismic waves to be detected.

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## ABSTRACT

Seismic detection apparatus comprising seismic detection means  
5 capable of detecting a plurality of seismic components over a  
defined tetrahedral volume is provided. The seismic detection  
means comprises four three-component geophones. Seismic data  
acquired by the geophones is processed to separate P-wave  
components from S-wave components. The geophones are spaced apart  
10 by distances smaller than the wavelength of the detected seismic  
components. The apparatus may be used on surface or in a marine  
environment or transition zone. A method of processing seismic  
data is also provided comprising acquiring seismic data relating to  
a wavefield over a selected volume of acquisition, and measuring  
15 the curl and divergence of the wavefield from the seismic data, to  
thereby identify seismic components within the seismic data.  
Additionally, an apparatus and method for hydrocarbon exploration  
is disclosed for using three or more seismic receivers placed in a  
plane and spaced closely to each other.

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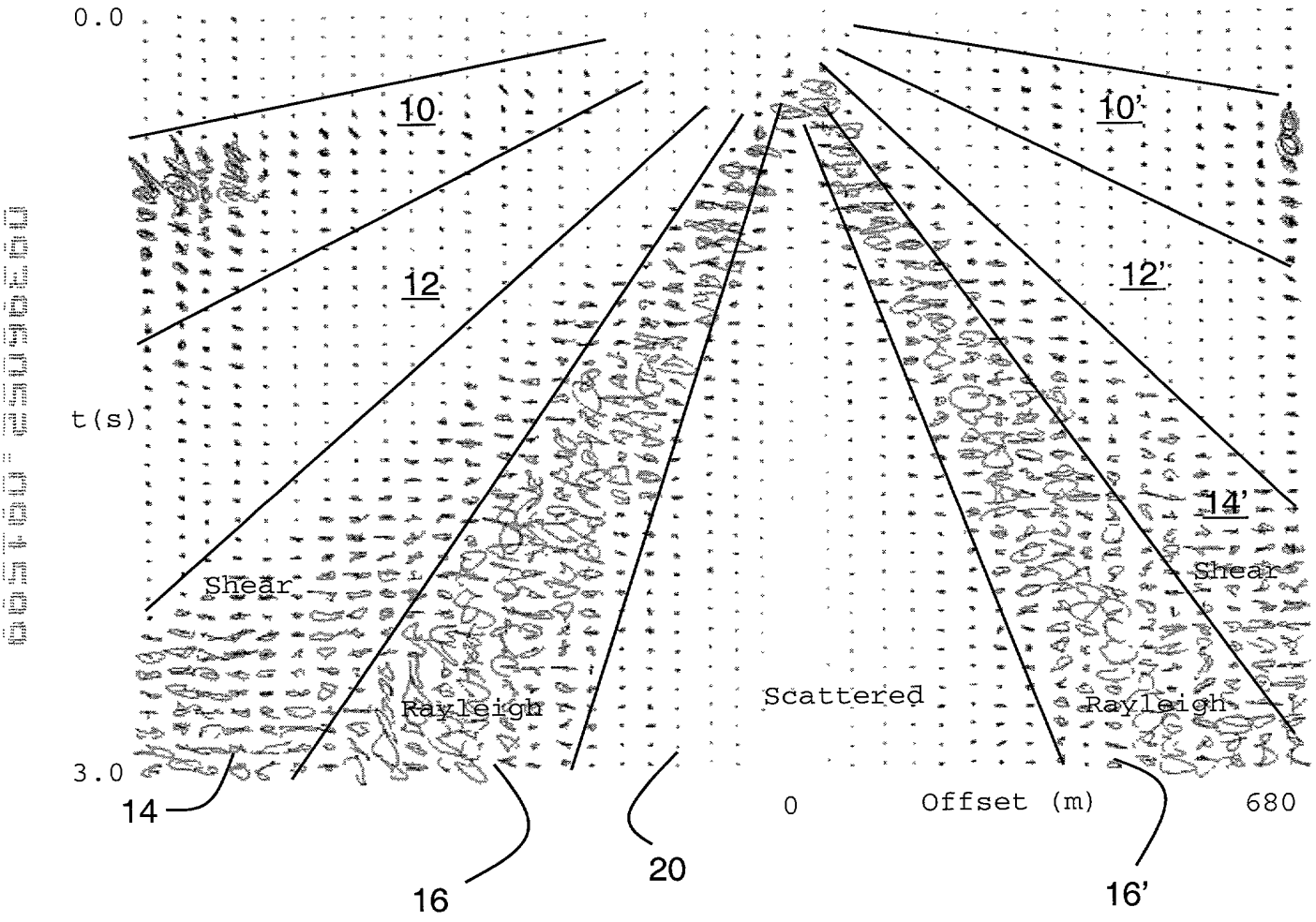


FIG. 1

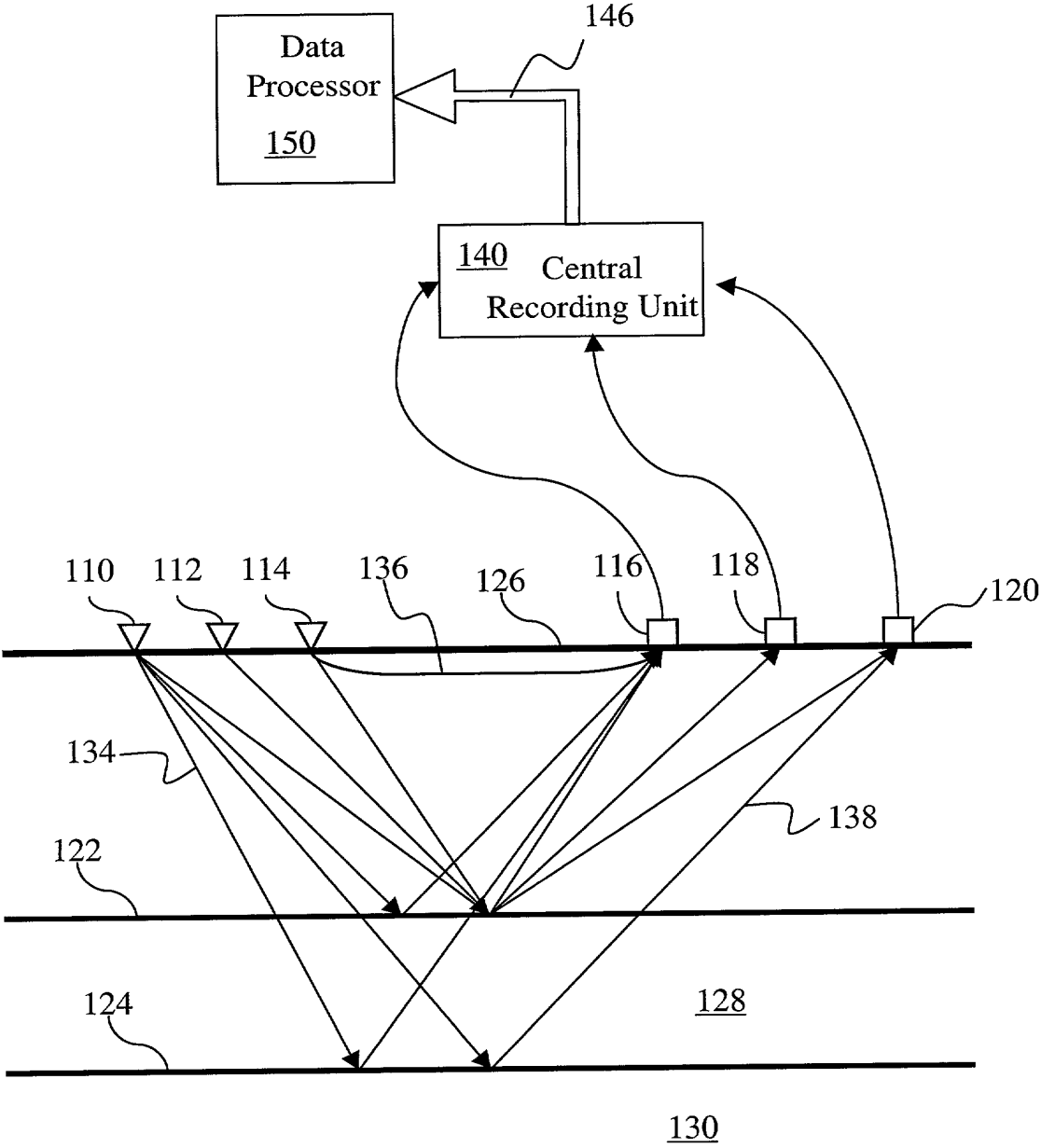


FIG. 2

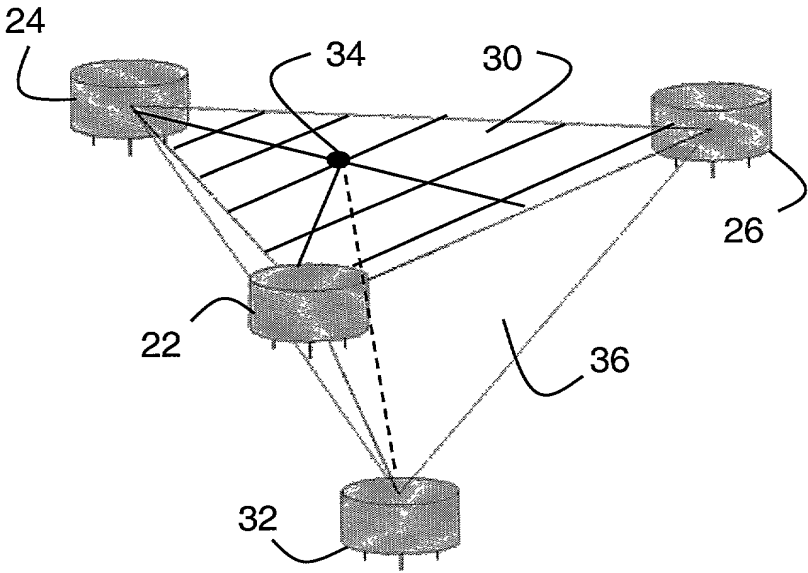


FIG. 3

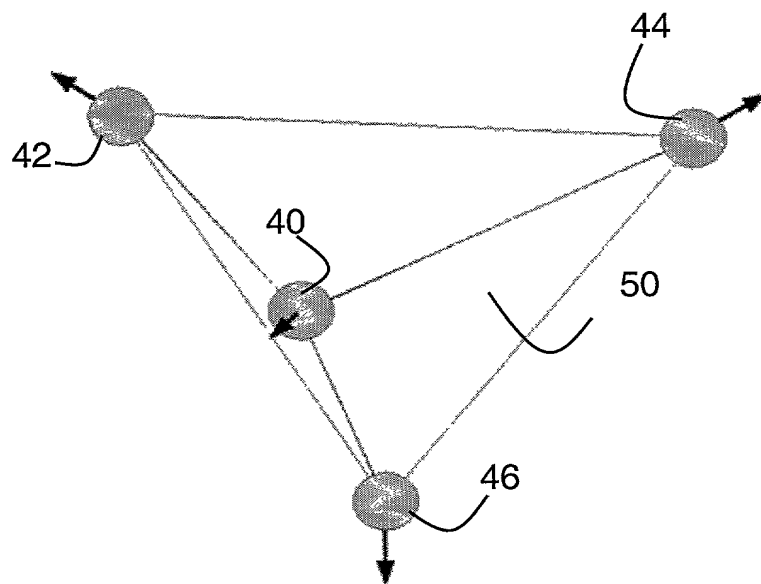


FIG. 4

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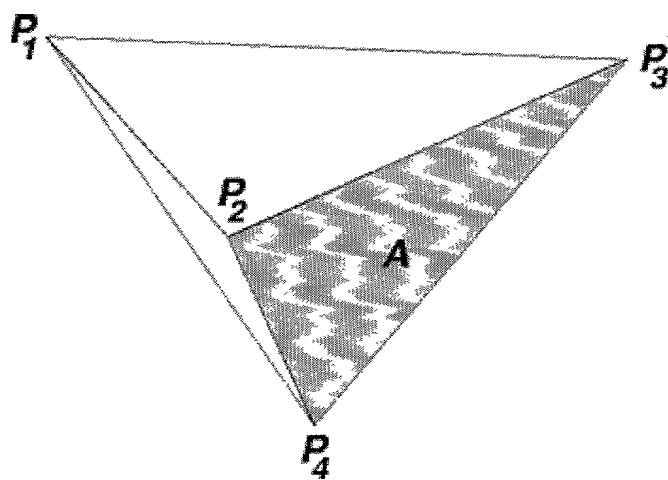


FIG. 5

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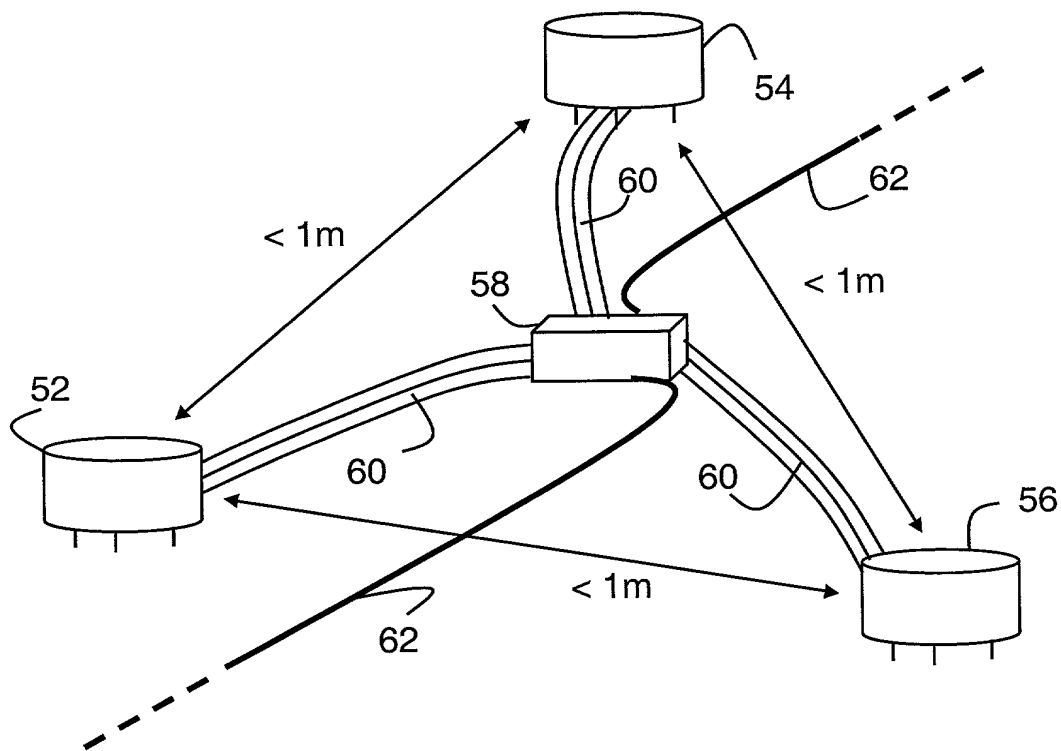


FIG. 6

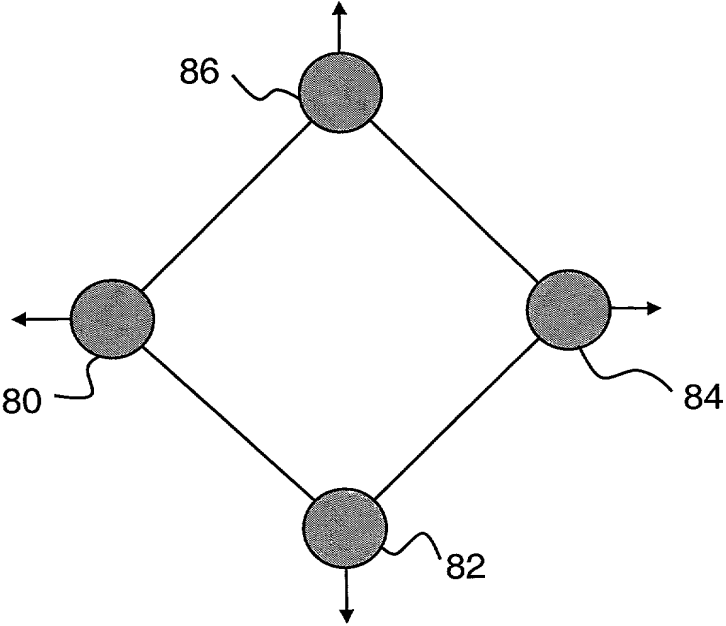


FIG. 7

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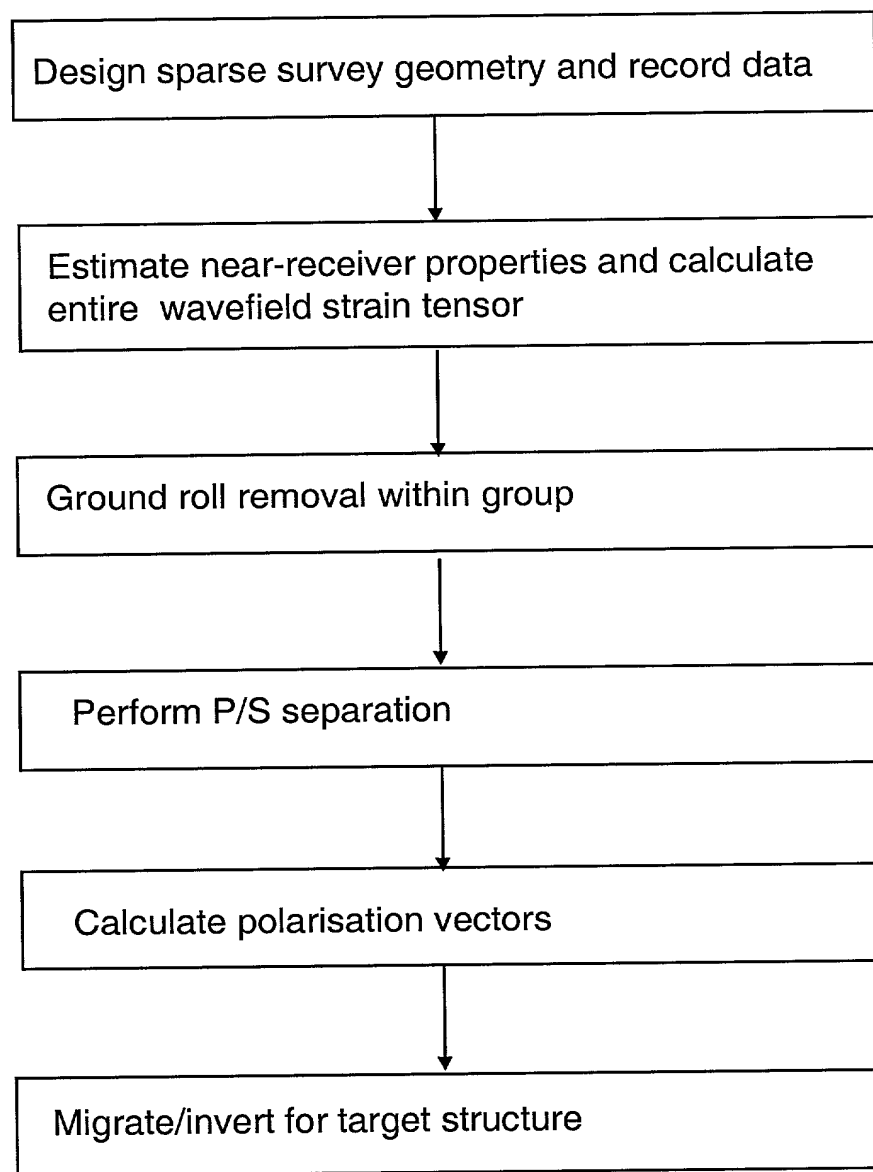


FIG. 8



## DECLARATION FOR PATENT APPLICATION AND POWER OF ATTORNEY

As a below named inventor, I/We hereby declare that:

My/Our residence, post office address(s) and citizenship(s) are as stated below next to my/our name(s), and

I/We believe I/We am/are the original, first and sole inventor of the subject matter which is claimed (if only one name is listed below) or an original and first inventor of at least some of the subject matter which is claimed (if plural names are listed below) and for which a patent is sought on the invention entitled

### SEISMIC DETECTION APPARATUS AND RELATED METHOD

the specification of which

☒ is attached hereto.

☐ was filed on

as Application Serial Number \_\_\_\_\_

and was amended on \_\_\_\_\_ (if applicable).

I/We hereby state that I/we have reviewed and understand the contents of the above identified specification, including the claims, as amended by any amendment referred to above.

I/We acknowledge the duty to disclose information which is material to the examination of this application in accordance with Title 37, Code of Federal Regulations, Section 1.56(a).

### Prior Foreign Application(s)

I/We hereby claim foreign priority benefits under Title 35, United States Code, Section 119 of any foreign application(s) for patent or inventor's certificate listed below and have also identified below any foreign application(s) for patent or inventor's certificate having a filing date before that of the application on which priority is claimed:

Country	Application No.	Filed (d/m/y)	Issued (d/m/y)	Priority Claimed
UK	9820049.6	(16 September 1998) 16.09.98		Y <input checked="" type="checkbox"/> N <input type="checkbox"/>
UK	9906995.7	(29 March 1999) 29.03.99		Y <input checked="" type="checkbox"/> N <input type="checkbox"/>

### Prior United States Applications

I/We hereby claim the benefit under Title 35, United States Code, Section 120 of any United States application(s) listed below and, insofar as the subject matter of each of the claims of this application is not disclosed in the prior United States application in the manner provided by the first paragraph of Title 35, United States Code, Section 112, I/We acknowledge the duty to disclose material information as defined in Title 37, Code of Federal Regulations, Section 1.56(a) which occurred between the filing date of the prior application and the national or PCT international filing date of this application:

Application Serial No.	Filing Date (d/m/y)	Status (Patented, Pending, Abandoned)

And, I/We hereby appoint, both jointly and severally, as my attorney(s) and/or agent(s) with full power of substitution and revocation, to prosecute this application and to transact all business in the Patent and Trademark Office connected herewith the following attorney(s) and agent(s), their registration numbers being listed after their names.

Peter Y. Lee, 30,865; John J. Ryberg, 31,134; William L. Wang, 39,871; and William B. Batzer, 37,088.

I/We hereby request that all correspondence be directed to:

Intellectual Property Law Department,  
Schlumberger-Doll Research,  
Old Quarry Rd., Ridgefield, CT 06877,  
and that all telephone calls be directed to Intellectual Property Law Department at (203) 431-5507.

I hereby declare (if sole inventor) or each of us hereby declares (if joint inventors) that all statements made herein of my own knowledge are true and that all statements made on information and belief are believed to be true; and further that these statements were made with the knowledge that willful false statements and the like so made are punishable by fine or imprisonment, or both, under Section 1001 of Title 18 of the United States Code and that such willful false statements may jeopardize the validity of the application or any patent issuing thereon.

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